

LETTER

Metacommunity-scale biodiversity regulation and the self-organised emergence of macroecological patterns

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Abstract

There exist a number of key macroecological patterns whose ubiquity suggests that the spatio-temporal structure of ecological communities is governed by some universal mechanisms. The nature of these mechanisms, however, remains poorly understood. Here, we probe spatio-temporal patterns in species richness and community composition using a simple metacommunity assembly model. Despite making no *a priori* assumptions regarding biotic spatial structure or the distribution of biomass across species, model metacommunities self-organise to reproduce well-documented patterns including characteristic species abundance distributions, range size distributions and species area relations. Also in agreement with observations, species richness in our model attains an equilibrium despite continuous species turnover. Crucially, it is in the neighbourhood of the equilibrium that we observe the emergence of these key macroecological patterns. Biodiversity equilibria in models occur due to the onset of ecological structural instability, a population-dynamical mechanism. This strongly suggests a causal link between local community processes and macroecological phenomena.

Keywords

biodiversity, ecological structural stability, macroecology, metacommunity, spatial ecology.

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INTRODUCTION

Despite the colossal diversity of environments where life is found across the globe, there exist a number of spatio-temporal patterns in biodiversity which are observed in almost every ecological community that has been studied. The species abundance distribution (SAD), which highlights the overwhelming predominance of rare species in ecological communities, has long been considered universal (Fisher *et al.* 1943; Preston 1948). A related pattern, the range size distribution (RSD), points to the prevalence of small (Brown *et al.* 1996; Gaston 1996), aggregated (Brown 1984) ranges, with few species occupying broad distributions. The species area relation (SAR), which denotes the sublinear increase in diversity as a function of sample area, has been described as 'one of community ecology's few genuine laws' (Schoener 1976).

The less extensively studied (and considerably more divisive) phenomenon of community-level diversity regulation, which constrains the number of species coexisting within an assemblage, has recently been proposed as a general ecological pattern (Gotelli *et al.* 2017; Magurran *et al.* 2018). Evidence of strong diversity regulation has been found in desert rodents (Brown *et al.* 2000), birds (Parody *et al.* 2001), marine fish (Magurran *et al.* 2015), freshwater communities (Magurran *et al.* 2018) and global-scale meta-analyses (Dornelas *et al.* 2014; Gotelli *et al.* 2017). At geological timescales, constrained diversification, assumed to reflect the impact of ecological limits on evolutionary processes, has been detected in the fossil record of a variety of taxa (Alroy 2009, 2010; Liow & Finarelli 2014; Benson *et al.* 2016; Close *et al.* 2019). Despite their apparent ubiquity, which strongly hints at some almost universal processes in macroecology, our mechanistic understanding of these

spatio-temporal patterns in biodiversity remains disparate and incomplete.

The theory of island biogeography (MacArthur & Wilson 1967) suggests that patterns in biodiversity may be explained as a consequence of the dependence of diversification rates – speciation, invasion and extinction – on standing diversity. In the 50 years since the Theory of Island Biogeography was first developed, however, the effects of environmental heterogeneity, landscape topography, local species interactions and dispersal have been shown to impact local and regional diversity patterns in complex ways (Shmida & Wilson 1985; Holt 1985; Pulliam 1988). Contemporary metacommunity ecology (Leibold *et al.* 2004; Holyoak *et al.* 2005; Logue *et al.* 2011; Winegardner *et al.* 2012) shines a light on how these complex and overlapping processes interact. Perhaps due to the persistent view that local and regional ecological processes cannot be meaningfully unified (Harmon & Harrison 2015), surprisingly few studies consider metacommunity frameworks that explicitly incorporate community dynamics at multiple spatial scales (e.g. Pillai *et al.* 2010; Barter & Gross 2017; but see Plitzko & Drossel 2015; Thiel & Drossel 2018). Here, we attempt to fill this gap with a dynamically simple metacommunity assembly model which incorporates local ecological interactions and dispersal in an environmentally heterogeneous landscape, thus uniting the branches of population-dynamical and spatial ecology. Our primary focus in developing this model was the study of how biodiversity might be regulated in spatially resolved ecological assemblages, but we find an intriguing emergent relationship between diversity regulation in model metacommunities and the appearance of widely observed macroecological patterns.

In spatially *unresolved* models, the emergence of biodiversity regulation has been observed numerous times (e.g. Drossel

et al. 2001; Yoshida 2003; Pawar 2009). Analytic theory (Rossberg 2013) reveals that this phenomenon is caused by the loss of *ecological structural stability*, which denotes the robustness of assemblages to press (i.e. sustained) perturbations (Meszena *et al.* 2006; Bastolla *et al.* 2005, 2009; Rossberg 2013; Rohr *et al.* 2014; Barbier *et al.* 2018). The mechanism is most easily understood for the paradigmatic case of Lotka–Volterra competition models of the form

$$\frac{db_i}{dt} = \left(r_i - \sum_j^S A_{ij} b_j \right) b_i \quad (1 \leq i \leq S), \quad (1)$$

with population biomasses b_i , intrinsic growth rates r_i , competition coefficients $A_{ij} \geq 0$ and species richness S . If all S species coexist ($b_i > 0$, for all i), the equilibrium condition for this system can be written in matrix-vector notation as $\mathbf{r} - \mathbf{A}\mathbf{b} = 0$ and is solved by $\mathbf{b} = \mathbf{A}^{-1}\mathbf{r}$. Mathematical problems of this form are called ‘ill conditioned’, implying that the solution \mathbf{b} responds sensitively to changes in both \mathbf{A} and \mathbf{r} , when some eigenvalues of \mathbf{A} approach zero. In ecological models, we define this sensitivity as ecological structural instability. Once this unstable condition arises, perturbation by external pressures or invaders, formally presentable by changes in \mathbf{A} or \mathbf{r} , can easily lead to extinctions. Structural stability (controlled by \mathbf{A}) and linear/Lyapunov stability (controlled by the Jacobian matrix) should not be confused. While these two phenomena are related (Stone 2018), each of them can independently control community structure and dynamics.

Random matrix theory of the kind invoked by May (1973), but applied to the competition matrix \mathbf{A} rather than the system’s Jacobian matrix at equilibrium, robustly predicts that with increasing species richness some eigenvalues of \mathbf{A} approach zero. The overall effect is thus that with increasing species richness structural instability increases, and accordingly, the likelihood that invasions cause species extinctions. Community assembly models, therefore, converge on dynamic steady states defined by the onset of structural instability. By applying alternative mathematical approaches to studying this phenomenon (Yodzis 1988; Tokita 2004; Rossberg 2013; Dougoud *et al.* 2018; Barbier *et al.* 2018; Galla 2018), structural instability can be interpreted as resulting from the amplification of perturbations through complex indirect interactions in large communities.

For other types of spatially unresolved community models, approximation techniques have been developed to map these onto competition models of the form eqn (1) (layered food webs: Bastolla *et al.* 2005, mutualistic communities: Bastolla *et al.* 2009, arbitrary food webs: Rossberg 2013), and the theory applies analogously. Whether this is similarly the case for metacommunity models is unknown. In order to understand the relationship between diversity regulation, potentially via the onset of ecological structural instability, and processes active in metacommunities, we constructed a multispecies framework in which metapopulation dynamics at the regional scale are modelled using a spatial network of Lotka–Volterra competition equations with additional terms describing dispersal (see *Dynamic equations and metacommunity assembly*, below).

By comparing the model’s behaviour to analytic predictions developed for spatially unresolved competitive communities

(Rossberg 2013), we show that intrinsic metacommunity-level diversity regulation can indeed be explained as a consequence of the onset of ecological structural instability at the *regional* scale. Surprisingly, and potentially very importantly, we find that, as model metacommunities approach diversity limits, they *self-organise* to reproduce macroecological patterns previously identified as central for the spatial structure of biodiversity (McGill 2010): a skewed local and regional distribution of abundances, spatial aggregation of conspecific biomass and apparent absence of species co-occurrence patterns. In combination, as McGill (2010) argued, these core patterns lead to sublinear species area relations and other spatial biodiversity phenomena. That a diverse set of well-known macroecological patterns emerges in a simple metacommunity model strongly supports the hypothesis that these patterns are indeed indirect consequences of local, niche-based population dynamics and dispersal.

RESULTS AND DISCUSSION

Metacommunity species richness

Simulated metacommunities, assembled in our model via a constant, slow influx of invaders, converge on regional diversity equilibria at which species richness remains approximately stationary despite continuous turnover in composition (Fig. 1). Diversity relaxes back to the same approximate steady state after sudden removal or introduction of large numbers of species (Fig. 1).

From previous theoretical work, we know that the sensitivity of a spatially unresolved community to press perturbations is a function of the standing diversity and the intensity of

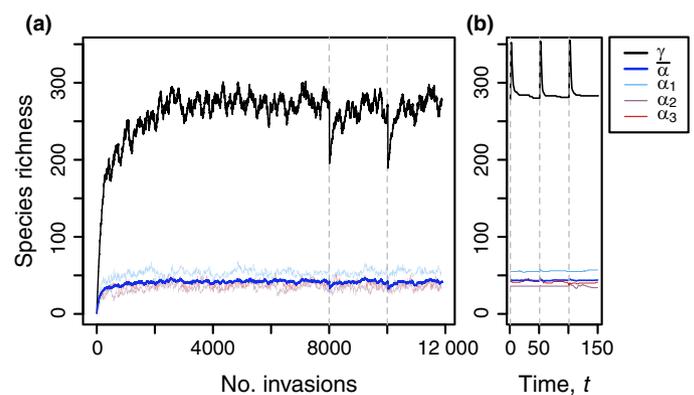


Figure 1 Biodiversity regulation in model metacommunities. The emergence of diversity equilibria at multiple spatial scales as a result of a stepwise invasion flux in a typical model metacommunity (a). Regional diversity (γ , black) and the average local diversity ($\bar{\alpha}$, blue) are shown, as well as that observed in three randomly selected patches (α , coloured). Relaxation back to equilibrium following random removal or introduction of large numbers of species (25% of the equilibrium richness, indicated by vertical dashed lines, a and b) reveals the strength and predictability of metacommunity-scale regulation in model assemblages. Relaxation times following removal and introduction differ by several orders of magnitude since the reaccumulation of diversity occurs at the invasion timescale, while extirpations occur at the population-dynamic timescale (measured in the units of t).

ecological interactions within that community (Rossberg 2013). The structurally unstable limit around which diversity in model communities converges, denoted S^* , is a function of the statistical distribution of the competition coefficients, typically their first and second moments (mean, variance, covariances). By assuming a precisely analogous mechanism to operate at the metacommunity scale, the basic spatially unresolved theory predicts an approximate regional diversity of

$$S^* \approx \frac{(1 - E[C_{ij}])^2}{2 \text{var}(C_{ij})} \quad (i \neq j), \quad (2)$$

(Rossberg 2013, eqn 17.5) where $E[C_{ij}]$ and $\text{var}(C_{ij})$ represent the expectation and variance of the interspecific competition coefficients computed at the scale of the metacommunity, replacing the distribution of local interaction coefficients A_{ij} in the spatially unresolved theory. The eigenvalue spectrum of the competitive overlap matrix offers a convenient graphical tool for assessing the ecological structural stability of community models. The structurally unstable diversity limit occurs as the area covered by the spectrum in the complex plane approach the origin (Rossberg 2013).

Regional scale, interspecific competition coefficients C_{ij} were computed for model metacommunities assembled for a range of parameter combinations, and used to evaluate eqn (2) (see *Regional scale interaction matrices, C* below). Comparing the diversity predicted by eqn (2) with that in the steady state of the simulation, we found that the spatially unresolved analytic prediction explains 95% of variance in the equilibrium species richness in the spatially resolved models (Fig. 2a). Furthermore, the spectra of the matrices C approach the origin when the biodiversity equilibrium is reached (Fig. 2b), just as observed in spatially unresolved models (Rossberg 2013). Thus, although an analytic prediction of the structurally unstable diversity limit in the metacommunity case is not available due to the intractability of the full model, we find strong evidence supporting the claim that ecological structural stability drives diversity regulation at the metacommunity scale.

The relationship between local and regional competition coefficients is non-trivial and depends on the degree of

environmental heterogeneity (see *Model landscape*, below). Nonetheless, we found the off-diagonal elements of A_{ij} and C_{ij} to be significantly correlated in metacommunity models at regional diversity limits ($P < 0.01$, for all parameter combinations). This implies that local ecological interactions propagate to the metacommunity scale and influence regional diversity patterns (Rabosky & Hurlbert 2015). For further discussion, see Supporting Information.

Local species richness

In order to distinguish between local and regional diversity, it is necessary to define some criterion for assessing presence–absence in a local assemblage. We do this in two ways. First by setting an arbitrary limit, equivalent to a detection threshold, of 10^{-4} biomass units below which a species is considered to be absent from a local community. This value is four orders of magnitude lower than the maximum local biomass permitted in the model and therefore defines a detectable range that is in accordance with many empirical observations (e.g. Condit *et al.* 2002). We further distinguish among those populations exceeding the detection threshold by defining *source* and *sink* populations as those capable of self-maintenance in a given location, and those that would decline without continuous immigration from adjacent communities (see *Source–Sink classification*, below).

During the assembly process (Fig. 1), we find that local community richness, defined by the detection threshold, saturates earlier than the regional assemblage (after around *c.*500 and *c.*4000 invasions, respectively, in the example shown). To confirm whether this local community regulation occurs independently of metacommunity regulation, it is necessary to ask how α -diversity is related to γ -diversity. If local diversity limits are controlled indirectly by the size of the regional species pool (i.e. regulation occurs meaningfully at one scale only), we would expect a linear, or at least non-saturating local–regional species richness relation. Interestingly, however, both source and sink diversity, and, by extension, their sum, are saturating functions of the regional species richness in equilibrium metacommunities. As we show in Fig. 3a, for which the distribution of interspecific coefficients A_{ij} was fixed across all

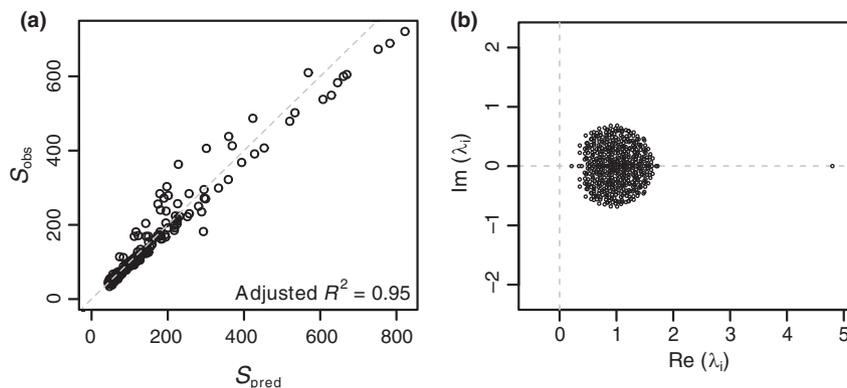


Figure 2 Testing for biodiversity regulation by structural stability in metacommunity models. (a) Comparison of the regional equilibrium diversity predicted by eqn (2) and that observed in simulated metacommunities for 195 combinations of patch number and spatial heterogeneity. The dashed line signifies equality. (b) The eigenvalue spectrum of a typical regional scale competitive overlap matrix C . Both analyses strongly suggest that the mechanism regulating diversity at the metacommunity scale is the loss of ecological structural stability.

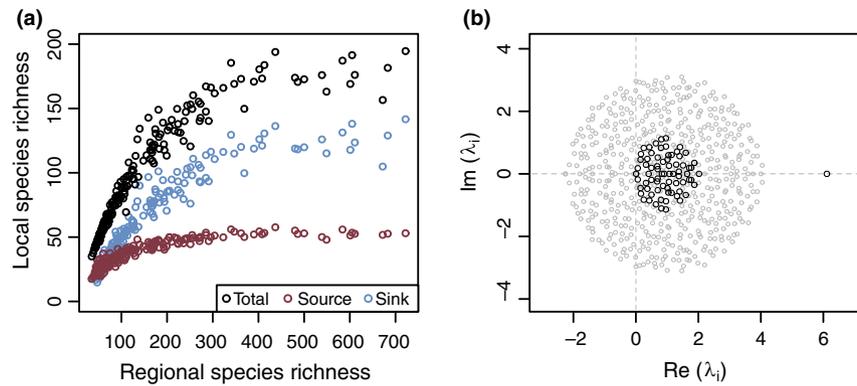


Figure 3 Demonstration of structurally unstable diversity regulation at the local scale. (a) Average local diversity (black), and that attributed to source (red) and sink (blue) populations, at regional diversity equilibrium, plotted against regional species richness for the same 195 parameter combinations used in Fig. 2. The sublinearity of the local–regional richness relation suggests that local communities are saturated with respect to both source and sink diversity for sufficiently high N . (b) Comparison of the spectra of the full competitive overlap matrix \mathbf{A} (grey circles) with that of its submatrix $\mathbf{A}_{\text{source}}$ (black circles) corresponding to source populations only, for a randomly selected local community at regional diversity equilibrium. The spectrum of $\mathbf{A}_{\text{source}}$ demonstrates the role of structural instability in regulating the diversity of the key, locally sustained component of the local assemblage.

simulations, and considering source populations only, average local diversity converged on a horizontal asymptote of $c.50$ once the regional assemblage reached $c.300$ species. Similar convergence, though with greater scatter, is evident for sink populations, though the asymptote may occur outside of the range studied here. This suggests that local diversity is indeed independently regulated, such that in sufficiently large regional communities local diversity is effectively independent of the metacommunity-scale parameterisation that determines the size of the regional species pool.

To explore the mechanism responsible for local diversity regulation we determined, for any given patch, the submatrix of \mathbf{A} corresponding to the local source populations only. We found that the spectra of these submatrices, too, approach the origin of the complex plane. Thus, we concluded that structurally unstable dynamics regulate species richness not only at the metacommunity level but also independently at the local level (Fig. 3b), and identified sink populations as the supersaturated component of the local assemblage, which depends on mass effects for persistence.

Temporal turnover

Stationarity in species richness is a key and unambiguous characteristic of our model metacommunities. Less obvious is the fact that, rather than converging on a near-static, ‘climax’ community, metacommunity composition in our models continuously turns over in response to the slow flux of invaders (Fig. 4a). Interestingly, on average, local communities turn over faster than the regional metacommunity of which they form a part. This is seen in the rapid decay in community similarity at the local, relative to the regional scale (Fig. 4a). This might be explained by range contraction and expansion due to regional biotic turnover which occur faster than landscape-scale competitive exclusion.

If the invader flux is spontaneously stopped and species are experimentally removed from the metacommunity in increasing order of regional biomass, fast turnover at local scales buffers local communities from the diversity losses at

metacommunity level (Fig. 4b). In the example shown in Fig. 4, a 20% decrease in regional species richness produced only a 13% drop at the local scale on average. It has been estimated that the current rate of global species loss is 100–1000 times the background rate (De Vos *et al.* 2015; Pimm *et al.* 2014; Ceballos *et al.* 2015), yet global meta-analyses have failed to detect a consistent loss of diversity at the local scale (Dornelas *et al.* 2014; Vellend *et al.* 2017; Gotelli *et al.* 2017). Our results suggest that independent regulatory processes operating at multiple spatial scales may account for the discrepancy between local and regional/global diversity trends.

Spatial patterns in biodiversity and abundance

By elegantly comparing the various major efforts to devise unified macroecological theory to date, McGill (2010) showed that three key macroecological phenomena are basic assumptions implicit to all frameworks. McGill argued that these key phenomena on their own are sufficient to give rise to a variety of emergent macroecological patterns, such as the sublinear SAR. The three key patterns are an uneven SAD at various spatial scales, the spatial aggregation of conspecific biomass underlying the observed skewed RSD, and the (apparent) non-significant correlation in species’ spatial distributions. The last phenomenon relates to the observation that statistically significant positive or negative correlations in species’ spatial distributions or co-occurrence patterns are surprisingly under-represented in empirical studies; most pairwise correlations tend to be indistinguishable from random (Hoagland & Collins 1997; Veech 2006; Houlahan *et al.* 2007; D’Amen *et al.* 2018). We find that, surprisingly, each of these three patterns emerges in our model metacommunities in the neighbourhood of regional diversity equilibria (Fig. 5).

Figure 5a shows that at both local and regional scale, the SAD are left-skewed log-normal, as observed in communities ranging from marine benthos to Amazonian rainforest (McGill *et al.* 2007). The early onset of diversity regulation at the local scale already leads to highly skewed SAD at the regional scale, after which further accumulation of diversity at

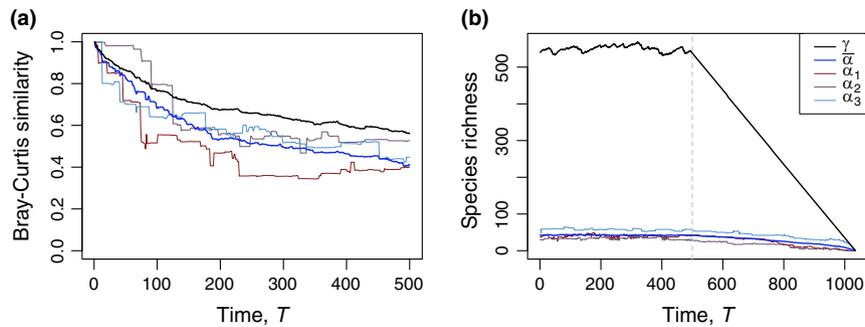


Figure 4 Temporal trends in community composition and species richness of model communities. The temporal Bray–Curtis similarity (a) and *source* population species richness (b, $T < 500$) for a metacommunity at regional equilibrium subject to a slow, discrete flux of invaders. Data for the metacommunity (black), the local average (blue) and three randomly selected local communities (coloured) are shown. After 500 invasions, the invasion flux in panel (b) is switched off and species are successively removed in order of increasing regional abundance.

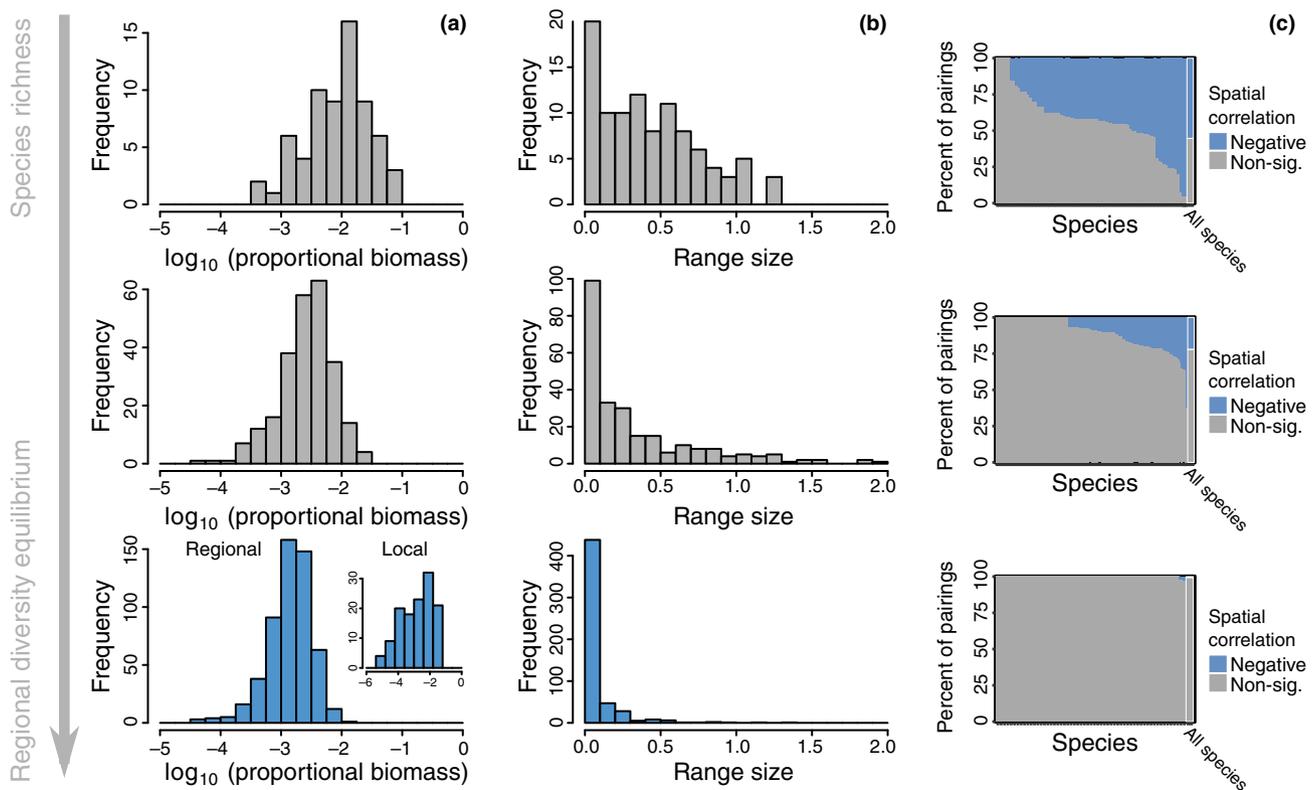


Figure 5 The effect of regional diversity regulation on macroecology in simulated metacommunities. Species Biomass Distributions (a), Range Size Distributions (b) and (c) Co-occurrence Profiles (Veech 2006; Griffith *et al.* 2016) for a typical model metacommunity at 20, 50 and 100% of the regional diversity equilibrium of around 500 species. In (b), an even distribution over the model landscape corresponds to a range size measure of 1.7, though for species concentrated near the edges our measure of range size can give even larger values. In (c), the percentage of possible species pairs that exhibit statistically significant ($P < 0.05$) negative spatial correlation is shown in blue for each species, and for the community as a whole (rightmost bar). Unsurprisingly, given the purely competitive nature of local ecological interactions, in our model metacommunities, no significant positive correlations were found. All three distributions converge on patterns well represented in the empirical literature as metacommunities approach the self-organised equilibrium.

the regional scale drives the distribution to the left as average biomasses decline.

In the early stages of the assembly process, as local diversity accumulates, weak biotic filtering means species disperse across much of their fundamental geographic niche. Once local communities become constrained, regional invasions instead drive an increase in spatial β -diversity, the ‘regionalisation’ of the biota (Ricklefs 2004) and a corresponding

reduction in species ranges, which become highly spatially aggregated. At the metacommunity scale, this is seen as a collapse in the RSD as the assemblage approaches regional diversity equilibrium (Fig. 5b). The skewed RSD for metacommunity models at regional diversity limits match patterns observed for a wide variety of taxa (Gaston 1998), including pine species (Brown *et al.* 1996), tropical tree species (Xu *et al.* 2015) and in both regional (Gaston 1996) and global

distributions (Orme *et al.* 2006) of bird species. Reduction in average range sizes and the corresponding increase in the number of effective interactions with neighbouring populations may increase species' vulnerability to regional extinction (Ricklefs 2004). As such we consider the emergent spatial aggregation in our metacommunity models to play an important role in regional scale diversity regulation.

The dependence of RSD on species richness implies a strong impact of ecological interactions on species ranges. Counter-intuitively, however, the vast majority of species pairs show no significant spatial correlation (Fig. 5c). As strong regional scale diversity regulation sets in and spatial ranges collapse, the percentage of species pairs for which it is possible to detect non-random spatial correlation drops to near zero, giving the impression of an eminently neutral system.

We considered the possibility that this absence of demonstrable spatial correlations is explained by the systemic exclusion of competing species pairs during assembly. However, for fully assembled model metacommunities at the regional diversity limit, non-zero interspecific competition coefficients made up 21.5–28.3% of the elements of the matrix A_{ij} , only 1.7–8.5% less than in the statistical ensemble from which invaders are sampled.

McGill (2010) argues that these three key phenomena (Fig. 5) can combine to produce sublinearity in the SAR. Recent non-dynamical modelling approaches have also shown that local community processes and spatial aggregation at the population scale can indeed reproduce high-level macroecological patterns (Rogge *et al.* 2018; Takashina *et al.* 2019). Here, we build on these results by showing that explicitly modelled population dynamics can drive spatial aggregation and produce the characteristic relationship between diversity and landscape area. The SAR in our models (Fig. 6) are well approximated by power laws with exponents ranging from 0.19 to 0.87, depending on the degree of spatial correlation in the model environment: a spatially more correlated, homogeneous environment produces an SAR with lower exponent. The exponents that emerge are well within the range found in a meta-analysis of almost 800 empirical SARs (Drakare *et al.* 2006). It has been shown (Rosindell & Cornell 2007; Pigolotti *et al.* 2018) that realistic SAR emerge in spatially explicit neutral models. Here we show, in light of evidence against neutral community assembly at regional scales (Ostling 2005), how sublinearity in the SAR can emerge via an explicit diversity-dependent mechanism.

CONCLUSION

There is a growing body of evidence indicating that community level diversity regulation is a common characteristic of ecological communities at both local and regional scales (e.g. Alroy 2009; Magurran *et al.* 2015, 2018; Gotelli *et al.* 2017; Dornelas *et al.* 2014). Proponents of this equilibrium paradigm concede that a precise mechanism explaining community regulation remains elusive (Magurran *et al.* 2018). Our numerical metacommunity model hints at a potential resolution to this problem and highlights an important avenue for the development of novel analytic theory. Inspection of recent results by Abernethy *et al.* (2019) for a spatially explicit food web model in the light of our observations suggests that the phenomena

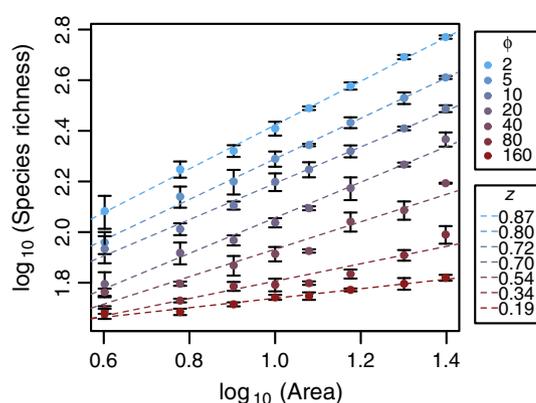


Figure 6 Species area relations for simulated metacommunities. Species richness increases as a function of model area according to approximate power laws with exponents ranging from 0.19 to 0.87. Colours indicate the degree of spatial environmental heterogeneity, ϕ . Error bars indicate standard deviations estimated from three independent model runs for each parameterisation, for which small differences between simulations arose largely due to the random topography of the model landscapes.

we observe are not restricted to competitive communities, but may apply to a wider range of ecological models.

With this study, we set out to assess the degree to which spatially unresolved ecological theory can incorporate the complex spatial processes occurring within model metacommunities. To our surprise, metacommunity models which explicitly incorporate dynamics at both local and regional scales reproduce an unprecedented range of empirically ubiquitous macroecological patterns. Crucially, these patterns result indirectly from the local dynamics, and in the neighbourhood of regional diversity limits. From this observation, we conclude that there is an important interaction between the system-scale dynamical process central to the theory of ecological structural stability and these key macroecological configurations. It is currently unclear precisely how structural instability at the metacommunity scale interacts with these key patterns. We suggest, therefore, that detailed studies of the mechanisms at work should be a priority of future research. We also note that the spatial decoupling of timescales we observe (Fig 4a) implies that for a metacommunity of sufficiently large spatial extent, regional ecological turnover could occur at timescales comparable to evolutionary or long-term environmental processes (e.g. glaciation cycles), as discussed by Ricklefs (2004). Because these processes are not included in our model, the 'regional' scale we refer to here must be understood as an intermediate spatial scale at which ecological processes operate comparatively fast.

If we conclude, on the basis of this and similar studies, that diversity regulation is indeed a common or general feature of ecological communities, this would entail a paradigm shift with important implications for the conservation and management of biodiversity. The assumption that local ecological dynamics have negligible impact on regional biotic distributions is still implicit in the majority of current conservation policies and programmes. Species distribution modelling (SDM) is a widely used method for identifying ecological processes and responses of species distributions to environmental change. The basic SDM methodology assumes that a

comprehensive understanding of current and future climate is sufficient to predict range shifts under climate change. Our results suggest that ignoring biotic interactions, even if they cannot be explicitly detected using conventional tools, may strongly undermine the effectiveness of these models (Wisz *et al.* 2013). As such, we suggest that the development and application of more mechanistic distribution modelling (Dormann *et al.* 2018) should be a priority, that management models might focus on higher levels of biological organisation (e.g. feeding guilds or entire communities), and that designers of conservation and management strategies make a concerted effort to integrate factors relating to diversity regulation in their decision-making.

METHODS

Model landscape

We generated a spatial network consisting of N patches by sampling the Cartesian coordinates (P_x, Q_x) of each patch x (with $1 \leq x \leq N$) from a uniform distribution in the range $(0, \sqrt{N})$. The local communities were thus randomly distributed with density ≈ 1 over a model landscape of area N . Corridors were defined using the Gabriel algorithm (1969) which connects nodes x and y if the disc with diameter given by the line segment xy contains no other nodes. This non-trivial topography is more realistic than a complete graph, but was also selected for its relative computational efficiency. In the limit of large N , the average patch degree does not exceed 4 (Matula & Sokal 1980), as for a square lattice, which will permit implementation of parallel simulation methods currently under development. Numerical experiments with fully connected graph lead to qualitatively similar emergent properties (see Supporting Information).

Environmental heterogeneity was modelled indirectly through spatial variation in species' intrinsic growth rates r_{ix} , where the subscript i is a species index, and x a patch index. The values of r_{ix} were sampled from a Gaussian Random Field (Adler 1981) ($\mu = 1.0$, $\sigma^2 = 0.5$), generated via spectral decomposition of the N by N landscape covariance matrix with elements $\text{cov}[\exp[-\phi^{-1}d_{xy}]]$, where d_{xy} denotes the Euclidean distances between two patches x and y , and the parameter ϕ controls the spatial autocorrelation of the environment (Johnson & Wichern 2002). By varying the correlation length ϕ while keeping mean and variance of the fields fixed, we modelled landscapes of varying degrees of environmental heterogeneity (see Supporting Information). Thus, though the environment is not explicitly modelled, the spatial autocorrelation of the environmental variables is expressed in the vectors \mathbf{r}_{ix} . A more detailed model would determine intrinsic growth rates indirectly from a match between spatially varying environmental variables and the species' Hutchinsonian niches. In our model, the spatially varying intrinsic growth rates are sampled directly for simplicity.

Parameters were chosen as $N = 10$, $\phi = 1$ for Fig. 1, $N = 20$, $\phi = 1$ for Figs 4 and 5. (Temporal decoupling of spatial scales is clearer in larger regional communities; however, for γ -diversity $\gg \alpha$ -diversity, it becomes difficult to represent local and regional assemblages on a single axis.) Figs 2, 3 and 6 summarise the complete parameter space studied: $N = 2, 4, 6, 8,$

10, 12, 15, 20 and 25; $\phi = 1, 2, 5, 10, 20, 40, 80$ and 160, in all combinations. Landscapes of $\phi > 160$ (in the spatial range studied here) showed no further decrease in regional species richness, or the exponent of the SAR, implying an effectively uniform environment.

Dynamic equations and metacommunity assembly

We used a spatial extension of the Lotka–Volterra multispecies competition equation to model local population dynamics and dispersal in our model metacommunities, thus building on the model family pioneered by Reichenbach *et al.* (2007). The rate of change in local biomass of species i at patch x is given by the nonlinear ordinary differential equation

$$\frac{db_{ix}}{dt} = b_{ix} \left(r_{ix} - \sum_{j=1}^S \mathbf{A}_{ij} b_{jx} \right) - eb_{ix} \quad (3)$$

The system of $N \times S$ coupled equations can therefore be written as

$$\frac{d\mathbf{B}}{dt} = \mathbf{B} \circ (\mathbf{R} - \mathbf{A}\mathbf{B}) + \mathbf{B}\mathbf{D}, \quad (4)$$

with \circ denoting element-wise multiplication.

The first term on the right hand side of eqn (3) represents the local dynamics, where \mathbf{A}_{ij} are the entries of the spatially unresolved competitive overlap matrix. In simulations, the off-diagonal entries \mathbf{A}_{ij} were sampled randomly, with \mathbf{A}_{ij} set to 0.3 with probability 0.3 and to 0 otherwise. The diagonal entries, representing intraspecific competition, were always set to 1. Together, eqn (2) and Fig. 2 imply that the critical diversity at which a model community converges depends only on the expectation and variance of the regional interspecific interaction coefficients. The details of the distribution from which the \mathbf{A}_{ij} are sampled do not enter the spatially implicit theory. For interaction matrices with pronounced structure (e.g. food webs), however, the underlying theory breaks down (Rossberg 2013). The impact of the distribution from which the local interactions \mathbf{A}_{ij} are sampled on spatial diversity patterns is subject of ongoing research.

The second term on the right of eqn (3) represents the rate at which biomass of species i emigrates away from patch x , while the third term gives the immigration rates from all patches y sharing an edge with x . The immigration rate decays exponentially with characteristic length ℓ , kept fixed at 0.2. The parameter e , which represents the fraction of biomass leaving patch x per unit time, was kept fixed at 0.02. An exploration of the parameter space of e and ℓ revealed little qualitative shift in the emergent properties of the model over the biologically relevant range (see Supporting Information), thus values were selected that favoured computational efficiency during model assembly. The normalisation constant k_y divides the biomass departing patches y between all other patches in the *its* local neighbourhood ($\mathcal{N}(y)$), weighted by the ease of reaching each patch, that is, $k_y = \sum_{z \in \mathcal{N}(y)} \exp(-d_{yz}\ell^{-1})$.

We adopted the community assembly modelling approach first developed by Post & Pimm (1983). In each iteration of the algorithm, a new species was added to the

metacommunity. Invaders were selected by computing the effective growth rate at low abundance of new species i with randomly generated ecologies (r_{ix} and \mathbf{A}_{ij}), until a species with positive growth rate in at least one patch was found. This was then added to the patch in which its effective growth rate was greatest with a low invasion biomass of 0.01 times the detection threshold of 10^{-4} biomass units. During invader testing, the competitive impact of the invader on the dynamics of resident species was set to zero, so that resident biomass was unaffected, to make sure we capture the invader's linear dynamics at low abundance. The metacommunity dynamics, including the spread of the new invader through the network and associated restructuring of the local resident biomass distribution, were then simulated using the SUNDIALS numerical ODE solver (Hindmarsh *et al.* 2005) over 500 unit times, t . Those species whose biomass dropped below the detection threshold in all patches of the network were considered regionally extinct and removed from the system. By thus iteratively adding species to the community, we modelled a constant flux of invaders, which causes the regional assemblage to self-organise, eventually converging on an equilibrium at which the invasion and extinction rates are equal on average. To reach this equilibrium, total simulation time was chosen as 4000, 6000, 8000, 10000 and 12000 iterations for $N \leq 4$, $6 \leq N \leq 10$, $12 \leq N \leq 15$, $N = 20$ and $N = 25$ respectively.

We note that \sqrt{N} determines the linear extension of the system, while ϕ and ℓ represent intrinsic length scales. There is a third intrinsic length scale, given by $1/\sqrt{\text{density of patches}}$, and this scale we kept fixed at 1. Because of this, there is no easy way to eliminate variables by rescaling lengths. It is conceivable that for very large system sizes N the discrete patch structure can give way to a continuum approximation with less parameters, but the question whether this is the case is beyond the scope of the present work.

Source–Sink classification

Source populations in a given patch x are those capable of locally maintaining themselves. Mathematically, source populations were defined as those for which local biomass was greater than the detection threshold and $r_{ix} - \sum_{j=1}^S \mathbf{A}_{ij} b_{jx} \geq 0$. Conversely, sink populations were those of biomass greater than the detection threshold and $r_{ix} - \sum_{j=1}^S \mathbf{A}_{ij} b_{jx} < 0$.

Regional scale interaction matrices, \mathbf{C}

In order to compare model metacommunity dynamics to theoretical predictions, we numerically computed a spatially unresolved competitive overlap matrix, denoted \mathbf{C} , that summarised the macroscopic dynamics at the regional scale. For this, we constructed a spatially *unresolved* Lotka–Volterra system,

$$dB_i/dt = \left(\rho_i - \sum_{j=1}^S \hat{\mathbf{C}}_{ij} B_j \right) \cdot B_i, \quad (5)$$

where B_i represents total biomass of species i , as an approximation of the spatially *resolved* model (eqn (3)). The aim of the following method is to arrive at a description of the effective interaction between pairs of species given the self-organised

spatial structure of metacommunity, which permits regional coexistence via spatial niche segregation. This requires integrating ecological interactions over the entire landscape, which was done using the computational equivalent of a harvesting experiment, under the assumption that interaction strengths can be inferred from the changes in regional abundances that result from controlled changes in the regional abundances of harvested species (Gilbert *et al.* 2014). Specifically, we asked how the steady state community responds to spatially unselective, light harvesting of a single species in the full model, and determined the coefficients $\hat{\mathbf{C}}_{ij}$ of the unresolved model such as to obtain identical responses to linear order in the harvesting rate.

$$\Delta B_j = -\hat{\mathbf{C}}_{ij}^{-1} h. \quad (6)$$

The most computationally efficient way of conducting the corresponding experiment for the meta community is to use a numerical approximation of the Jacobian matrix. In doing so, we assume simulated metacommunities to be at fixed points, an approximation that is justified retrospectively by the apparent efficacy of the method. In fact, large metacommunity models begin to manifest periodic or irregular oscillations, a potentially important phenomenon which is the subject of ongoing research. For the present study, we limited our numerical experiments to those spatial ranges in which such autonomous fluctuations are absent or weak, such that the numerical Jacobian represents a reasonable approximation of the dynamic coupling within the system and can be used to compute a time-independent, regional scale interaction matrix which meaningfully describes the structural stability of the metacommunity. The elements of the Jacobian are given by the general equation

$$\mathbf{J}_{ixjy} = \frac{\partial f_{ix}(b_{11}, \dots, b_{S1}, \dots, b_{1N}, \dots, b_{SN})}{\partial b_{jy}}, \quad (7)$$

evaluated at equilibrium. The functions f_{ix} denote the right hand side of eqn (3).

Light harvesting of a single focal species i at a rate h brings about a small shift in the equilibrium biomasses of the other species in the metacommunity and the dynamics of the harvested community *near the unharvested equilibrium* (b_{jy}^*) can be approximated by

$$\frac{db_{ix}}{dt} = \left(\sum_{jy} \mathbf{J}_{ixjy} (b_{jy} - b_{jy}^*) \right) - hb_{ix}^*, \quad \text{and} \quad (8a)$$

$$\frac{db_{kx}}{dt} = \left(\sum_{jy} \mathbf{J}_{kxjy} (b_{jy} - b_{jy}^*) \right) \quad \text{for } k \neq i. \quad (8b)$$

here, h is the harvesting rate. We vectorise the matrix \mathbf{B} (denoted $\vec{\mathbf{B}}$) such as to match the dimensionality of the spatially resolved Jacobian, and write the equilibrium condition for eqn (8a) as

$$\mathbf{J}(\vec{\mathbf{B}} - \vec{\mathbf{B}}^*) - \vec{\mathbf{H}} = 0, \quad (9)$$

where the elements of vector $\vec{\mathbf{H}}$ are hb_{jy}^* for $j = i$ and 0 otherwise. From this, we obtain

$$h^{-1}(\vec{\mathbf{B}} - \vec{\mathbf{B}}^*) = \mathbf{J}^{-1}h^{-1}\vec{\mathbf{H}}. \quad (10)$$

The left hand side of eqn (10) represents the local shift in biomasses due to the harvesting of the focal species i per unit h . From eqn (10), we compute the change in total biomass $\Delta B_j = \sum_x b_{jx} - b_{jx}^*$ for each species j . Comparison with (6) gives row i of $\hat{\mathbf{C}}^{-1}$. Iterating over all species $i = 1 \dots S$, we computed $\hat{\mathbf{C}}^{-1}$ and from this the spatially unresolved interaction matrix $\hat{\mathbf{C}}$. Finally, in order to match the assumptions made in the derivation of eqn (2) (Rossberg 2013), we divided each row and column $\hat{\mathbf{C}}$ by the square root of the corresponding diagonal element to obtain the *effective competitive overlap matrix*, \mathbf{C} (which has ones along the diagonal).

Temporal diversity patterns

Temporal species richness and turnover in community composition were computed for a metacommunity at regional diversity limits for a period corresponding to 500 ecological invasions (Fig. 4). Species richness analysis requires the application of some presence–absence criterion. We assess local community diversity by reference to the source populations only, since sink populations are effectively decoupled from local filtering processes by dispersal.

Following the 500 invasions, species were removed in reverse order of regional abundance, in order to model a large-scale mass extinction process. A single metacommunity of $N = 20$, $\phi = 2$ was used for this analysis.

Compositional turnover in metacommunities at regional diversity equilibria was measured using the Bray & Curtis (1957) similarity. An arbitrary initial metacommunity composition was selected ($T = 0$ in Fig. 4a) and the relative compositional change computed in the context of a constant invasion flux using the function `vegdist` in the R package ‘vegan’ (Oksanen *et al.* 2018). In order to generate Fig. 4a, regionally excluded or as yet uninvaded species were assigned biomass vectors with all elements set to zero.

Species ranges

In order to quantify range sizes of species, we first computed, for each species i , the population covariance matrix

$$\Sigma_i = \begin{pmatrix} \text{var}(P_x) & \text{cov}(P_x, Q_x) \\ \text{cov}(P_x, Q_x) & \text{var}(Q_x) \end{pmatrix} \quad (11)$$

of the locations (P_x, Q_x) of individuals forming the species’ population, assuming population sizes are proportional to biomasses at each patch. For example, with i being the index of the focal species, $\text{var}(P_x) = B_i^{-1} \sum_x b_{ix} (P_x - \bar{P}_x)^2$, where $B_i = \sum_x b_{ix}$ is total biomass, as above, and $\bar{P}_x = B_i^{-1} \sum_x b_{ix} P_x$ is the P component of the centre of mass of the distribution. Correspondingly, $\text{var}(Q_x) = B_i^{-1} \sum_x b_{ix} (Q_x - \bar{Q}_x)^2$, $\text{cov}(P_x, Q_x) = B_i^{-1} \sum_x b_{ix} (P_x - \bar{P}_x)(Q_x - \bar{Q}_x)$, with $\bar{Q}_x = B_i^{-1} \sum_x b_{ix} Q_x$. As a measure of range size, we computed the product of the square roots of the eigenvalues of Σ_i , that is, the square root of its determinant, $\sqrt{|\det \Sigma_i|}$. By this measure, an even distribution of biomass over the full $\sqrt{N} \times \sqrt{N}$

rectangle enclosing one of our model communities corresponds to a range size of $N/12$.

Species co-occurrence

In order to analyse the correlation in species spatial distributions within our model landscapes, we used the probabilistic model developed by Veech (2013) included in the R package ‘cooccur’ (Griffith *et al.* 2016). The observed pairwise co-occurrence is computed as the probability of detecting species i in patch x given the detection of species j in that local community, which is then compared to that expected if two species were distributed independently within a discretised landscape.

AUTHOR CONTRIBUTIONS

AGR conceived of the study. JDO and AGR designed the model. JDO developed the model, performed simulations, analysed the data and drafted the manuscript. All three authors interpreted model outputs in comparison with observations and contributed to manuscript writing. The authors declare no competing interests.

DATA ACCESSIBILITY

Simulation data supporting the results can be found online from the Figshare Repository: <https://doi.org/10.6084/m9.figshare.8114195.v2>.

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SUPPORTING INFORMATION

Additional supporting information may be found online in the Supporting Information section at the end of the article.

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Supporting Information

The coupling of local and regional competition coefficients

The interaction between environmental gradients and competitive overlap coefficients in the determination of the regional overlap coefficients \mathbf{C}_{ij} is complex and depends upon the degree of environmental heterogeneity. To test the hypothesis that local interactions (\mathbf{A}_{ij}) drive regional community assembly (Rabosky and Hurlbert, 2015) we need to analyse the extent to which fundamental and realised competitive overlap coefficients are correlated. Simple linear regression shows that \mathbf{A}_{ij} and \mathbf{C}_{ij} are indeed significantly correlated ($p < 0.01$, for all parameter combinations), but the strength of the correlation, measured by the adjusted R^2 , ranges from 0.1 to 1.0.

Unsurprisingly, given the nature of \mathbf{C} , the slope of the relationship $m \leq 1$, with $m \sim 1$ in the homogeneous extreme (high ϕ and/or low N , Fig. S1A), in which case the strength of the correlation between local interactions and regional community assembly is maximised (Fig. S1B).

Spatial structure at the metapopulation scale

The combined effect of local and regional diversity regulation drives spatial turnover in community composition. Species in model metacommunities near regional limits converge on highly aggregated spatial distributions in which biomass decays exponentially as a function of distance from regional maxima (Fig. S2, note the logarithmic colour gradient).

Regional scale competitive overlap matrices

Fig. S3A-B highlights the difference in magnitude of the regional scale interaction coefficients, which incorporate the complex spatial coexistence mechanisms active in heterogeneous landscapes. Spatial coexistence mechanisms in model metacommunities can be understood as slowing the onset of structural instability by modifying the distribution in spatially resolved competitive overlap coefficients. The spectrum of the ‘microcosmic’ competitive overlap matrix \mathbf{A} (Fig. S3C), fully covering the origin of the complex plane, highlights the fact that such an assemblage would be biologically unfeasible in the absence of the abiotic (topographical and environmental) variation in the model.

Spatial autocorrelation in maximum intrinsic growth rates

Spatially correlated intrinsic growth rates r_{ix} were modelled using a Gaussian random field as described in *Model landscape*. Fig. S4 shows four complete realizations of spatially distributed growth rates, r_{ix} , generated using autocorrelation lengths $\phi = 1$ and 10.

Dispersal parameterization and landscape topography

The numerical experiments conducted in this study, focused on a single point in the parameter space of e , and ℓ (0.02,0.2). In practice the parameterization was selected in order to maximize the computational efficiency of the assembly process. Here we show that the self-organized spatial structure of strongly regulated model metacommunities is robust to changes in the dispersal parameters within a biologically meaningful parameter space. Figs. S5 and S6 show the regional diversity, average local source and sink richness, and the skew of the RSD, for a model metacommunities ($N = 20$, $\phi = 1$) assembled using parameters e and ℓ spanning four orders of magnitude, with each parameter combination triple replicated.

In both cases the regional diversity increased slightly as a function of ℓ in the case $e < 1$. This results contrasts with that observed, for example, by Mouquet and Loreau (2003), who find that in the high dispersal regime, metacommunities tend to converge on monoculture. In our model system, environmental heterogeneity (here high), ensures that no species can dominate the entire landscape. The weak *increase* in diversity suggests that dispersal limited rare species may be rescued from regional extirpation by increasing landscape connectivity. In the case $e > 1$, which implies $e > \bar{r}_{ix}$, the regional diversity is significantly reduced and an approximate monoculture does indeed emerge in the high dispersal regime, as the metacommunity approaches the patch-dynamics paradigm assumed by Mouquet and Loreau (2003).

The average local source richness is largely unaffected by dispersal parameterization in the case $e < 1$ since this component is instead strongly regulated by local ecological dynamics. In the case $e > 1$, all populations depend in immigration from adjacent patches and the average local source diversity drops immediately to zero.

The average local sink richness depends strongly on parameterization, and landscape topography. For $e < 1$ sink richness increases as a function of dispersal length until the combined source and sink diversity approaches on the regional species richness, a scenario in which most species have a detectable population in all local communities. This

result is qualitatively comparable to that observed by Bastolla et al. (2001), who showed how island diversity increases as a result of super-saturation due to fast immigration from a continental species pool. In the case $e > 1$ it is difficult to meaningfully interpret source-sink dynamics, since in this extreme dispersal regime, all populations depend on immigration for persistence. It is only in this extreme case that we observe consistent deviation from what is arguably the key macroecological property of our model metacommunities - a regional biota with an RSD that is positively skewed.

Our study focuses on the parameter space in which γ -diversity is large compared to mean α -diversity, implying meaningful spatial turnover in community composition. While investigation of systems in which dispersal effectively homogenizes local communities is interesting, it is outside of the scope of this study. In the parameter space of interest here (the highlighted region in Figs. S5 and S6) we consider the diversity patterns to be qualitatively robust.

The choice to employ the Gabriel graph *as well as* an exponential dispersal kernel, enforces dispersal limitation in two potentially conflated ways. As described in section *Model landscape*, this was largely a pragmatic choice. We are confident, however, that macroscopic properties of the metacommunity do not depend on the topography of the network. Comparison of Figs. S5 and S6), shows how, the non-trivial patch adjacency reduces average sink diversity by effectively reducing the average range within the assembly. The qualitative patterns, however, are not strongly impacted and as such we surmise the emergent phenomena depend more on the ecological, than the topographic network.

References

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- D. L. Rabosky and A. H. Hurlbert. Species richness at continental scales is dominated by ecological limits. *The American Naturalist*, 185(5):572–583, 2015.
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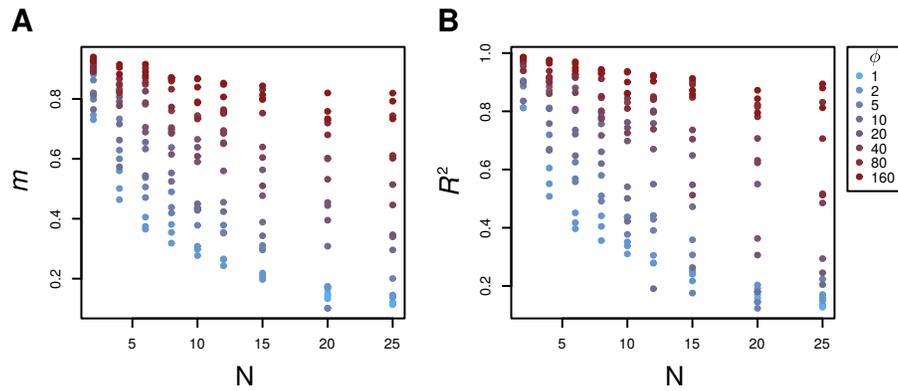


Figure S1: **The statistical relationship between interspecific competitive overlap coefficients A_{ij} and C_{ij} .** The slope of the linear regression of the elements of C_{ij} against those of A_{ij} (A) and the adjusted R^2 of the relationship (B). Colours denote to environmental auto-correlation length, ϕ .

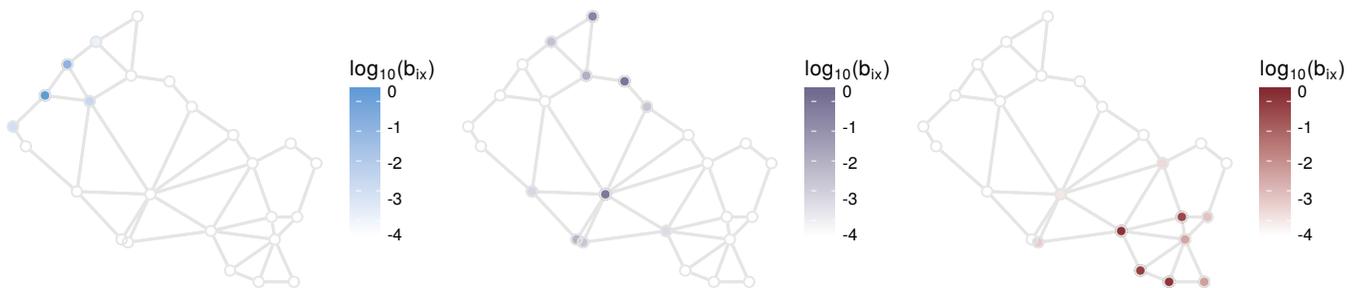


Figure S2: **A typical spatial model landscape and the distribution of biomass for three simulated species.** Dispersal corridors (gray links) in random spatial networks were assigning using the Gabriel Algorithm. Colours correspond to three randomly selected species biomass distributions. Spatial aggregation is a key characteristic of species ranges in strongly regulated metacommunities.

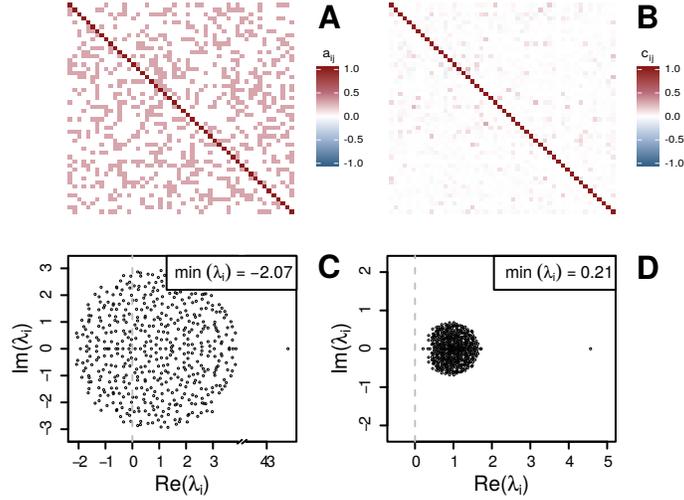


Figure S3: **Comparison of the matrices \mathbf{A} and \mathbf{C} for a single metacommunity at regional diversity equilibrium.** The local competitive overlap matrix \mathbf{A} (A) and regional *effective* competitive overlap matrix \mathbf{C} (B) for a randomly sampled subset (for visual clarity) of a typical model metacommunity ($N = 20$, $\phi = 1$) at regional diversity equilibrium and the corresponding eigenvalue spectra (C and D). The off-diagonal elements, \mathbf{C}_{ij} , incorporate the effects of both spatial segregation and ‘indirect mutualism’ (which can lead to negative values). The spectrum of the regional overlap matrix \mathbf{C} , which approaches the origin as diversity saturates, matches that observed in spatially unresolved models (Rossberg, 2013).

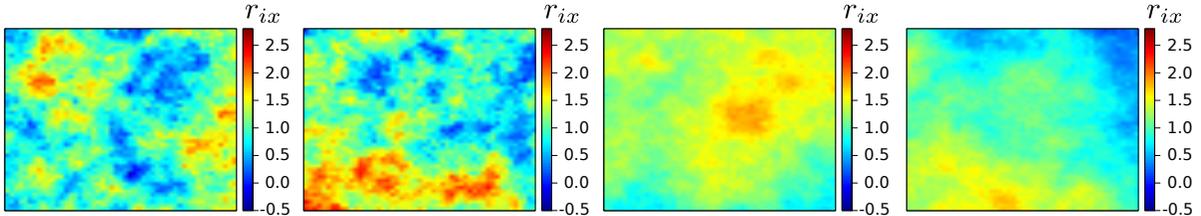


Figure S4: **Spatially autocorrelated Gaussian random fields used in environmental modelling** Four complete realization of Gaussian random fields generated via eigen-decomposition of the spatial covariance matrix. The ‘landscapes’ shown here have side lengths of $\sqrt{20}$ and spatial correlation lengths, ϕ , of 1 (left) and 10 (right).

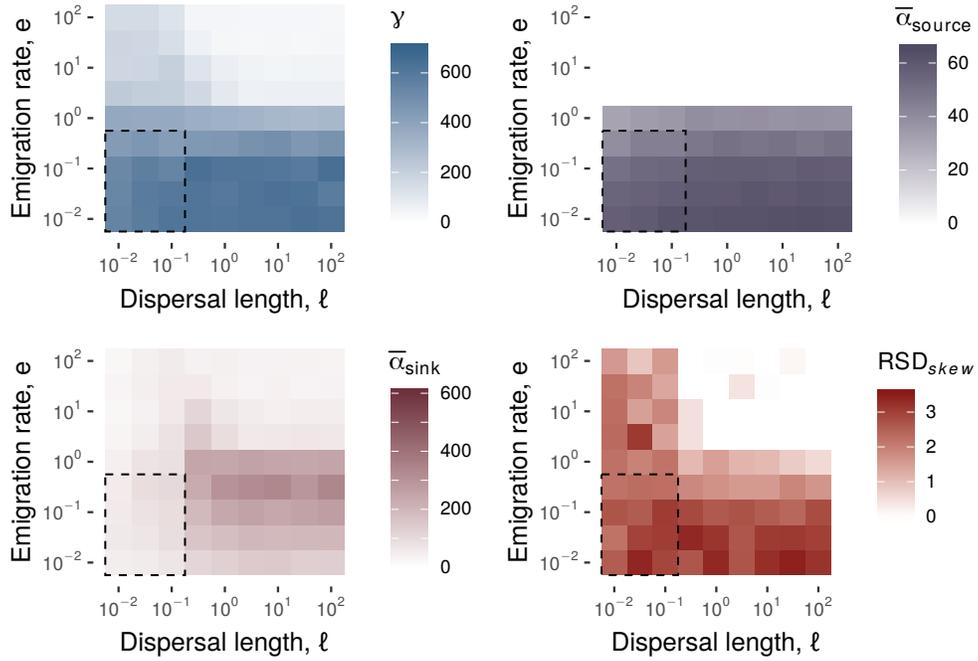


Figure S5: **Regional, average source, and sink species richness, and the skewness of the RSD under variation of e and ℓ , for the Gabriel graph.** Exploration of the parameter space of the dispersal parameters shows that our results are qualitatively robust to variation in e and ℓ in the biologically relevant regime indicated by the dashed box. See text for further details.

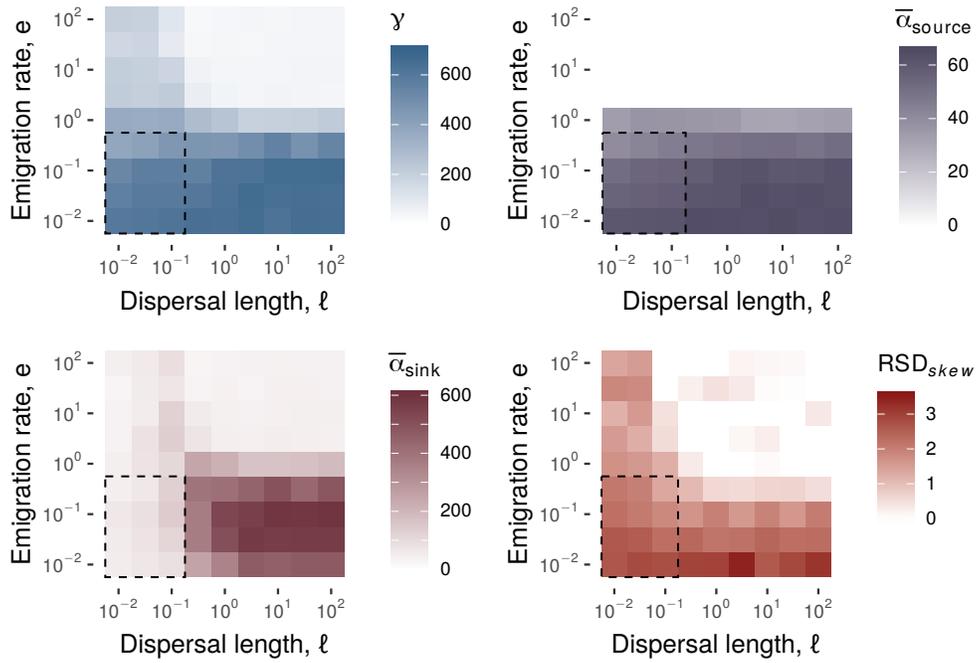


Figure S6: **Regional, average source, and sink species richness, and the skewness of the RSD under variation of e and ℓ , for the Complete graph.** As in Fig. S5, for fully connected random graphs.